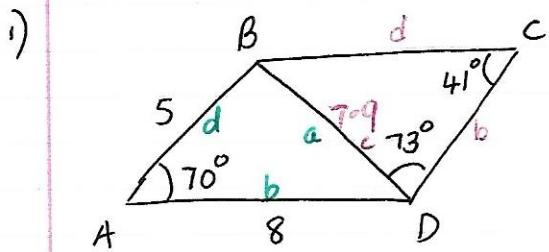


Year 10 Trig. in 2 Stages : Answers



Use $\triangle ABD$

$$\begin{aligned}a^2 &= b^2 + d^2 - 2bd \cos A \\BD^2 &= 8^2 + 5^2 - 2(8)(5) \cos 70^\circ \\BD^2 &= 64 + 25 - 80 \cos 70^\circ \\BD^2 &= 89 - 80 \cos 70^\circ \\BD^2 &= 89 - (27.36)\end{aligned}$$

$$BD^2 = 61.64$$

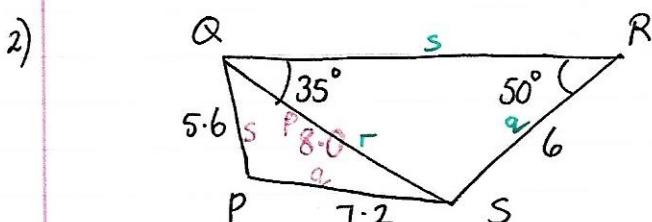
$$BD = 7.9 \text{ cm}$$

Now use $\triangle BCD$

$$\begin{aligned}\frac{b}{\sin B} &= \frac{c}{\sin C} = \frac{d}{\sin D} \\\cancel{\frac{b}{\sin B}} &= \frac{7.9}{\sin 41^\circ} = \frac{BC}{\sin 73^\circ}\end{aligned}$$

$$\frac{7.9 \sin 73^\circ}{\sin 41^\circ} = BC$$

$$11.5 \text{ cm} = BC$$



First
Use $\triangle QRS$

$$\begin{aligned}\frac{q}{\sin Q} &= \frac{r}{\sin R} = \frac{s}{\sin S} \\\frac{6}{\sin 35^\circ} &= \frac{QS}{\sin 50^\circ} = \cancel{\frac{s}{\sin S}} \\\frac{6 \sin 50^\circ}{\sin 35^\circ} &= QS\end{aligned}$$

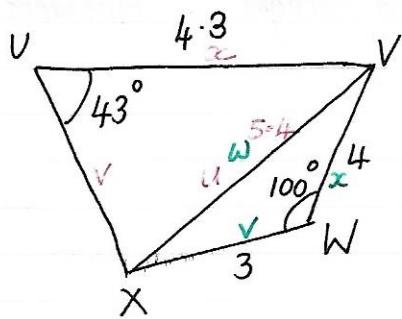
$$8.0 \text{ m} = QS$$

Now

$\triangle PQS$

$$\begin{aligned}s^2 &= p^2 + q^2 - 2pq \cos \hat{P}SQ \\5.6^2 &= 8^2 + 7.2^2 - 2(8)(7.2) \cos \hat{P}SQ \\31.36 &= 64 + 51.84 - 115.2 \cos \hat{P}SQ \\115.2 \cos \hat{P}SQ &= 84.48 \\\cos \hat{P}SQ &= 0.73 \\\hat{P}SQ &= 42.8^\circ\end{aligned}$$

3)

First ΔVWX

$$\begin{aligned}\omega^2 &= x^2 + v^2 - 2uv \cos W \\ \omega^2 &= 4^2 + 3^2 - 2(4)(3) \cos 100^\circ \\ \omega^2 &= 16 + 9 - 24 \cos 100^\circ \\ \omega^2 &= 25 - (-4 \cdot 17)\end{aligned}$$

$$\omega^2 = 29 \cdot 17$$

$$\omega = 5.4 \text{ m}$$

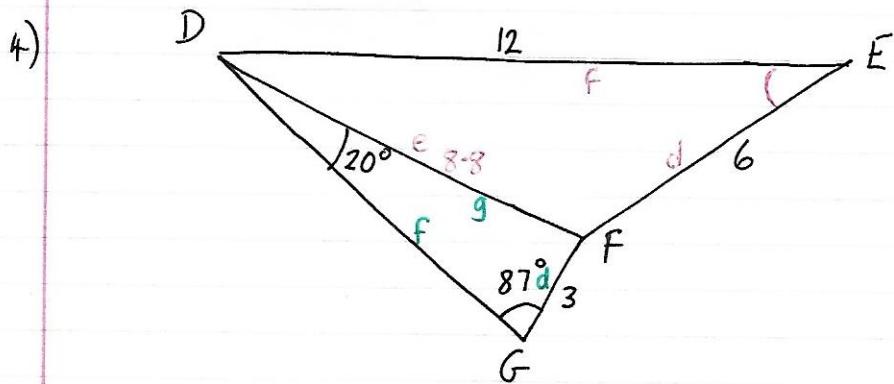
Now ΔUVX

$$\begin{aligned}\frac{u}{\sin V} &= \frac{v}{\sin V} = \frac{x}{\sin X} \\ \frac{5.4}{\sin 43^\circ} &= \frac{v}{\sin V} = \frac{4.3}{\sin \hat{U}X\hat{V}} \\ \frac{\sin 43^\circ}{5.4} &= \frac{\sin \hat{U}X\hat{V}}{4.3}\end{aligned}$$

$$\frac{4.3 \sin 43^\circ}{5.4} = \sin \hat{U}X\hat{V}$$

$$0.543 = \sin \hat{U}X\hat{V}$$

$$32.9^\circ = \hat{U}X\hat{V}$$



Use $\triangle DFG$

$$\frac{d}{\sin D} = \frac{f}{\sin F} = \frac{g}{\sin G}$$

$$\frac{3}{\sin 20^\circ} = \frac{f}{\sin F} = \frac{g}{\sin 87^\circ}$$

$$\frac{3 \sin 87^\circ}{\sin 20^\circ} = DF$$

$$8.8 \text{ cm} = DF$$

Now use $\triangle DEF$

$$e^2 = d^2 + f^2 - 2df \cos E$$

$$8.8^2 = 6^2 + 12^2 - 2(6)(12) \cos \hat{D}\hat{E}\hat{F}$$

$$77.44 = 36 + 144 - 144 \cos \hat{D}\hat{E}\hat{F}$$

$$144 \cos \hat{D}\hat{E}\hat{F} = 102.56$$

$$\cos \hat{D}\hat{E}\hat{F} = \frac{102.56}{144}$$

$$\cos \hat{D}\hat{E}\hat{F} = 0.712$$

$$\hat{D}\hat{E}\hat{F} = 44.6^\circ.$$